

# ASSESSMENT OF SENSITIVITY OF PUSHOVER ANALYSIS

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## Abstract

In this present study, an attempt has been made to determine the uncertainty occurring in pushover analysis results for a Reinforced Concrete (RC) G+2 storied frame modeled as a bare frame and frame with rigid diaphragm slab by considering user-defined hinges using non-linear static pushover analysis using SAP2000. Since the output of the analysis is very much sensitive and susceptible to design parameters, to interpret the sensitivity analysis by varying the strength of steel, concrete and hinge lengthon the performance of structures and compare the variation in the performance which is randomly generated and incorporated into the analysis. The nonlinear behavior of the elements was modeled using plastic hinges based on the moment-curvature relationship as described in Federal Emergency Management Agency (FEMA)-356 and Applied Technology Council (ATC)-40. A seismic response like base shear, roof displacement corresponding to performance point was evaluated using nonlinear static analysis. The experimental results were compared with analytical results.

**Keywords:** Non-Linear Static Pushover Analysis, Lateral Load, Concrete and Cover, Moment-Curvature Analysis, Hinge Length.

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## 1. INTRODUCTION

The intent of Pushover analysis is to assess the expected performance by analysing its strength and deformation requirements in the seismic design of structure by using Non-linear static analysis and evaluating these requirements to accessible capacities at important performance levels. The utilization of non-linear study is vital to represent the performance of buildings under earthquake action as observed by Mehmet Inel and Ozmen (2006) [2]. In past, many types of research works have been achieved on traditional non-linear analysis and after inspecting flaws, attempts have been developed to better the results. Ashraf Habibullah et al (1998) [1] suggested the practical steps used to perform the pushover analysis in SAP2000 software. It documents the approach for modeling and defining the criteria for a hinge as per ATC-40 and FEMA documents. Krawinkler and Seneveritna (1998) [6] conferred about advantages and disadvantages of the Pushover analysis. They assessed the accuracy of the method and recognized the cases in which the pushover predictions are unreliable.

Much improvisation is required, combined with experimentally obtained results and analysis stressed by S.Elnashai (2001) [7]. But the experimental test results are rarely available to correlate with pushover analysis. In the present study, the analytical results are being correlated with experiment results which were conducted in Structural Engineering Research Center (SERC), Chennai.

## 2. EXPERIMENTAL SPECIFICATIONS

The experiment test as shown in figure.1 was performed by Akanshu Sharma at SERC, Chennai. Servo-hydraulic actuators was used to propel the RC frame to take reaction. The load distribution was parabolic along the height. The experiment was conducted governed by

increasing monotonic pushover loads with the load distribution being parabolic along the height of the structure. The maximum base shear was 286.5kN and corresponding roof displacement was 0.110m.



**Fig-1:** Experimental System for Pushover Test

In this paper, keeping the basis of experimentally obtained results of corresponding base shear and roof displacement, the frame structure is modeled in SAP 2000 program and analyzed to inspect the sensitivity of pushover curve.

### 3. DESCRIPTION OF THE STRUCTURE

#### 3.1 Sectional Details

The structure is G+2 storeyed RC framed structure. Fig.1 shows actual test structure.

Column dimension- 150mm× 200mm

Beam dimension- 150mm× 200mm

Reinforcement- Beam – 2-12 Φ at top

2-16 Φ at bottom

Column– 2-16 Φ at top

2-16 Φ at bottom

Stirrups– 6 Φ @150mm c/c for beams and

column

Slab thickness- 50mm

The average concrete strength of the tested structure- 35Mpa

The average reinforcement yield stress of the tested structure – 478Mpa

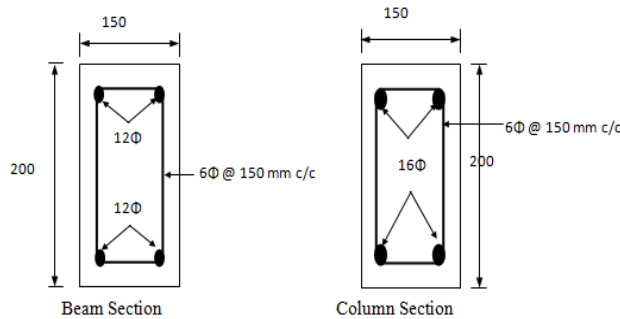


Fig-2:Sectional Properties of Beam and Column

#### 3.2 Modelling Details

Material and geometrical properties are assigned as per the experimental structure and a basic model is generated in SAP2000. Different inbuilt default and user defined plastic hinge options are available in SAP2000 based on average values from ATC-40 [6] and FEMA-273 [8] for concrete members and steel members respectively. As the user-defined hinges reflect elemental nonlinearity behaviour, user-defined hinges are preferred over default hinge options. To use user-defined hinge properties selection moment-curvature analysis of each element is required. Moment-curvature values are generated based on a material model for concrete and steel. In the present study, IS suggested stress-strain model for unconfined concrete and British code (CP-110-1972) for steel have been adopted as shown in figure 3 and figure 4. The generated values of moment-curvature of beam and column are shown in table 1 and table 2. Moment values are in kN-m.

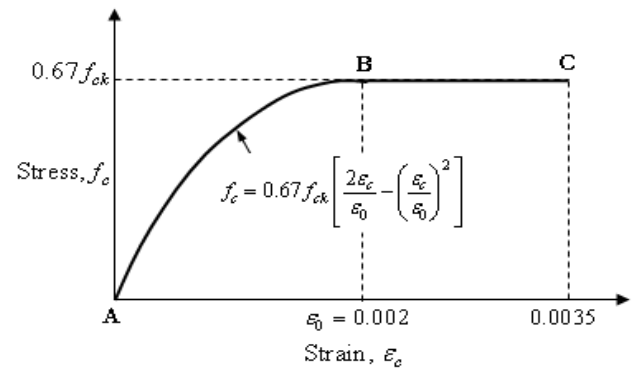


Fig-3: IS suggested stress-strain model for unconfined concrete

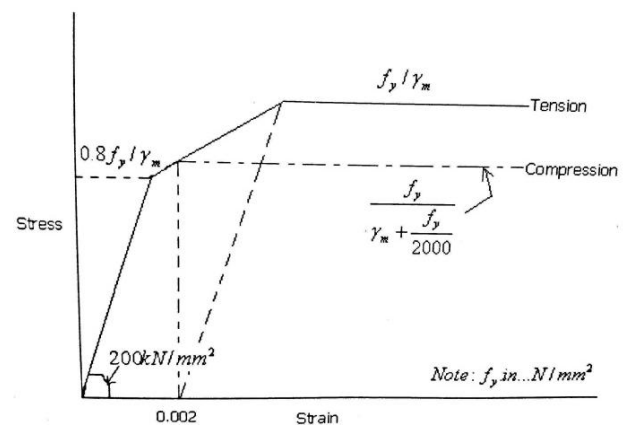


Fig-4: Stress-strain curve for steel suggested by British code

#### 3.3 Load Calculations

After modeling the structure, pushover load cases are defined. Generally, after applying gravity load as the first pushover load case, then following lateral pushover load is applied to start from the final state of gravity loading. Structures along the height of the structure are subjected to lateral loads, which are based on the formula in Eq. (1), in FEMA 356 [4], shown below and then incorporated in the model.

$$\begin{aligned}
 \bullet \quad F_x &= \frac{W_x h x^k}{\sum_{i=1}^N W_i h_i^k} V \\
 \bullet \quad C_{vx} &= \frac{W_x h x^k}{\sum_{i=1}^N W_i h_i^k}
 \end{aligned}
 \tag{1}$$

Where  $F_x$  is lateral load applied at any floor level “x”,  $W$  is total building weight,  $h$  is the floor height,  $V$  is lateral load and  $N$  is the number of floors.  $C_{vx}$  is vertical distribution

Table-1: Moment-curvature data for beams

Points	A	B	C	D	E
	Origin	Yielding	Ultimate	Strain-hardening	Strain-hardening
$f_y = 478 \text{ N/mm}^2$ $f_{ck} = 35 \text{ N/mm}^2$	$M=0$ $\Phi=0$	$M=13.8$ $\Phi=0.0126$	$M=14.04$ $\Phi=0.0748$	$M=14.82$ $\Phi=0.0801$	$M=16.9$ $\Phi=0.0951$

**Table-2:** Moment-curvature data for columns

Points	A	B	C	D	E
	Origin	Yielding	Ultimate	Strain-hardening	Strain-hardening
$f_y=478\text{N/mm}^2$ $f_{ck}=35\text{N/mm}^2$	M=0 $\Phi=0$	M=23.0 $\Phi=0.0148$	M=23.9 $\Phi=0.0915$	M=24.92 $\Phi=0.098$	M=27.79 $\Phi=0.1183$

factor for the lateral load. Using the above equation, the lateral loads were calculated. The lateral loads were applied in the ratio of 9:4:1 on each floor as generated by above equation and then applied to the model.

#### 4. ANALYSIS AND RESULTS

The preliminary analysis was performed by taking into the account of the material properties which were used in experiment and considering bare frame and rigid diaphragm slab was done in SAP2000. From the analysis performed, it was observed that for the bare frame model the base shear

(P) and corresponding displacement ( $\Delta$ ) was found to be 167kN and 0.268m respectively and for rigid diaphragm slab, the base shear (P) and corresponding displacement ( $\Delta$ ) was found to be 276kN and 0.172m respectively. Thus, from the analysis results obtained, it is evident that the experiment results vary to analysis results. Hence, from the obtained results, the pushover analysis for material and geometric modeling are sensitive and susceptible. The percentage difference of base shear and displacement is shown in table.3.

**Table-3:** Percentage difference of base shear and displacement

Frame	Base Shear (kN)	Percentage less than experiment	Displacement (m)	Percentage more than experiment
Bare Frame	167	41.7%	0.268	143.6%
Rigid Diaphragm slab	276	3.6%	0.172	56.3%

The plastic hinge length is an important design parameter where extreme confinement should be provided to increase the ductility of the member for the extreme seismic action. Further investigation is carried out to check the possible variation in the results obtained from pushover analysis by adopting bare frame and rigid diaphragm slab model by calculating hinge length using different hinge length properties available in the literature by considering user-defined hinges. Various different formulations have been suggested for calculating the corresponding user-defined plastic hinge lengths  $L_p$ . The length of the user-defined hinge is considered from the following formulations,

1. Corley's formula

- $L_p = 0.5d + 0.2\sqrt{d}\left(\frac{z}{d}\right)$

2. Park's formula

- $L_p = 0.42h$

3. Priestly-Park's formula

- $L_p = 0.8z + 6d_b$

4. Panagiotakos-Fardis's formula

- $L_p = 0.18z + 0.021d_b f_y$

5. Berry's formula

- $L_p = 0.05z + \left(\frac{0.1dbf_y}{\sqrt{f_c}}\right)$

Where,

$d_b$  = diameter of longitudinal reinforcing bars, in mm

$f_y$  = yield stress of reinforcing bars, in  $\text{N/mm}^2$

$z$  = Critical section distance from the point of contra-flexure, in mm

$d$  = effective depth of the cross section, in mm

$h$  = Overall depth of the cross section, in mm

$f_c$  = compressive strength of concrete, in  $\text{N/mm}^2$

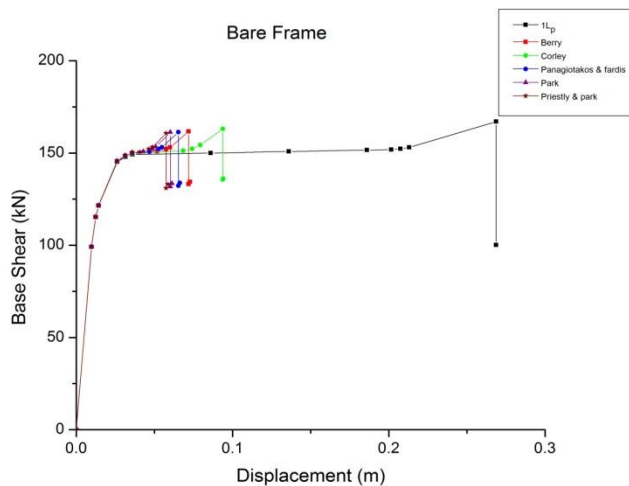
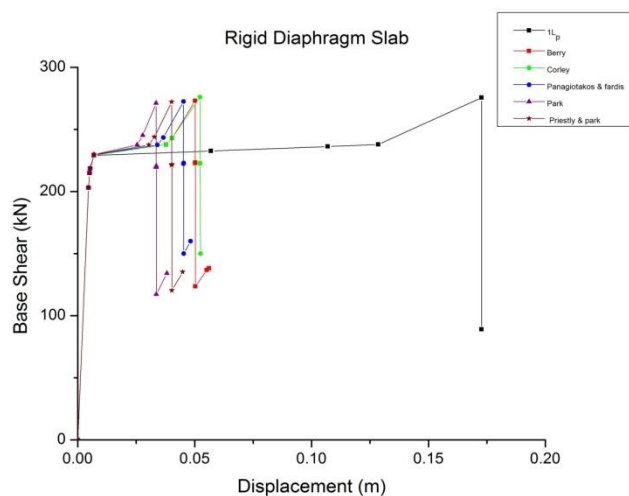
Using above formulations by considering user-defined hinge option the bare frame and rigid diaphragm slab was analyzed. The pushover analysis results are shown in table.4 and table.5 respectively. The comparative graphs of pushover curves for different hinge length are shown in figure.5 and figure.6 respectively. From the graph, base shear and displacement were not much varied but when different hinge length properties were considered, it was observed that there was a large difference in base shear and displacement.

**Table-4:** Base Shear and Displacement Values for Bare frame

Formulations	Base Shear (kN)	Displacement (m)
Berry	161.62	0.072
Corley	163.06	0.093
Panagiotakos and Fardis	161.27	0.065
Park	161.18	0.060
Priestly and Park	160.66	0.057

**Table-5:** Base Shear and Displacement Values for Rigid Diaphragm slab

Formulations	Base Shear (kN)	Displacement (m)
Berry	272.89	0.050
Corley	273.89	0.051
Panagiotakos and Fardis	272.50	0.045
Park	271.15	0.033
Priestly and Park	272.08	0.040

**Fig-5:** Comparison of Pushover curve for different hinge length (Bare frame)**Fig-6:** Comparison of Pushover curve for different hinge length (Rigid Diaphragm slab)

## 5. CONCLUSION

- In bare frame model, it was observed that values of Base Shear values were low, whereas values for displacement were high due to slab stiffness was not considered.
- For bare frame model, Base Shear variation was found to be 40-46% lesser than experiment values and Displacements about 15-48% less.
- For Rigid Diaphragm slab model, Base shear was found 4-5% lesser than experiment values and Displacement about 53-70% less.
- For Bare frame model considering hinge length formulations, comparing with experiment values, both base shear and displacement values were less.
- For Rigid Diaphragm slab model considering hinge length formulations, comparing with experiment values, the base shear was nearer while displacement was less.
- Therefore, Non-linear static pushover analysis results are greatly sensitive and susceptible to changes made in geometrical modeling, material properties, hinge length properties etc and precise efficient analysis method is required to predict the experimental results with the analysis for more accurate results.

## ACKNOWLEDGEMENT

I would take this opportunity as a privilege to thank my family and my respected guide Dr. PoornachandraPandit to their continuous guidance, inspiration and support, which are main factors behind any work. I take the pleasure of thanking all those who have helped, supported and gave constant encouragement throughout my work without whom, this work would not have been completed in time.

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