A SIMULATION STUDY OF WiMAX BASED COMMUNICATION SYSTEM USING DELIBERATELY CLIPPED OFDM SIGNAL

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Abstract
WiMAX is a highly sophisticated technology in the broadband wireless access communication system. Scalable Orthogonal Frequency Division Multiple Access (OFDMA) is a key technology behind mobile WiMAX and it is also expected to play a key role in 3GPP Long Term Evolution (LTE) standards. Designers and OEMs have to concentrate on flexibility, scalability and stability of the overall Orthogonal Frequency Division Multiplexing (OFDM) system along with its proper data processing and channeling process to achieve high performance and competitiveness. In this paper, the performance of a strictly band limited OFDM signal is examined using deliberate clipping method, one of the simplest signal distortion based way to reduce high Peak to Average Power Ratio (PAPR) and its effect on the resultant Bit Error Rate (BER) against Signal to Noise Ratio (SNR) performance. A simulation program using MATLAB software was developed to investigate performance of OFDM signal by optimization of different parameters such values of FFT size, Cyclic Prefix co-efficient (CPC) and The Voltage Clipping Ratio (VCR). The simulation results show that with the increment of VCR at optimized parameter values of FFT size and CP, the performance of BER vs SNR improves compared to the results found without clipping.

Keywords: WiMAX, PAPR, OFDM, CPC, Voltage Clipping Ratio, Deliberately Clipped

1. INTRODUCTION TO WiMAX TECHNOLOGY

Wireless communications have become increasingly popular and broadly required in today’s fast-paced world, specially for the people of developing countries like Bangladesh. Instant access to virtually unlimited information and resources has become the way of life for individuals in different sectors of living and earning their livelihood. Access to various forms of information such as image, data, voice, video and multimedia in an easily communicable, secure and in cost-effective manner are the basic requirements of modern day technology savvy society.

Wi-Fi (IEEE Standards based 802.11) has dominated as the most popular wireless access technology within the home and office since 2005 due to its cheaper hardware price, easy to use and interoperability within a range of 30 meters. When used in Metropolitan Area network (MAN) the operation of Wi-Fi started to face challenges for its range, QoS and security. Standard Wi-Fi technology is limited to 100m range in Line-of-Sight (LOS) environment which in the pre-release versions of 802.11n got standardized to 250m by the use of MIMO Antenna at both Access Point and The Subscriber Station [1]. Despite all the developments, Wi-Fi remains limited to LAN space in terms of range and depends on WAN technologies to bridge the last miles to access internet and external connectivity.

Broadband Cellular Wireless (BCW) system thus appears as the technique to satisfy this rapidly growing demand of communication systems. A key benefit of it is the ability to use bidirectional antennas which results in improved strength of signal on both directions. The standards 802.16d and 802.16e popularly known as WiMAX (Worldwide Interoperability for Microwave Access) become a key technology in mitigating the previous issues of range. Since the late 90s, WiMAX technology based communication system has been addressed by the IEE802.16 group which was formed in 1998 to develop an air-interface standard for wireless broadband. The original 802.16 standard was based on single carrier physical (PHY) layer with a burst Time Division Multiplexed (TDM) Machine Access Control (MAC) layer. After the IEEE 802.16 group subsequently produced 802.16a (an amendment to the standard), to introduce NLOS applications in the 2GHz–11GHz band, using OFDM based PHY layer with additional support of OFDMA in the MAC layer. In December 2005, the IEE group completed and approved IEEE 802.16e-2005, an amendment which added mobility support and forms the basis for the WiMAX solution for mobile applications referred as mobile WiMAX [2]. And the WiMAX forum has been formed to promote the interoperability between manufacturers and vendors for the conformance to the standard.
2. ORTHOGONAL FREQUENCY DIVISION MULTIPLEXING (OFDM)

Mobile WiMAX uses OFDM as a multiple access technique which is a joint process of modulation and multiplexing.

In OFDM, multiplexing operation is performed on independent signals which are a sub-set of the one main signal. The signal first itself is split into independent channels, modulated by data and then multiplexed to create the OFDM carrier.

The main concept in OFDM is Orthogonality of the sub-carriers. As all the sub-carriers are sine or cosine wave, area under one period of sine or cosine wave is zero and the area under a sine wave multiplied by its own harmonic is always zero. Thus orthogonality allows simultaneous transmission on a lot of sub-carriers in a restricted or tight frequency space without being interfered with each other. In this way, it is quite similar to the technique adapted in CDMA where codes are used to make data sequences independent (also orthogonal) and allowing many independent users to transmit in same space successfully.

2.1 Applications and Parameters of real OFDM System

OFDM is a vastly adapted data multiplexing technique for high speed networks and has gradually increased in commercial usage over the last decade. It is now proposed for radio broadcasting such as in Eureka 147 standard and Digital Radio Mondiale (DRM) [3]. OFDM is used for modem/ADSL application where it co-exists with phone line which is called Discrete Multi Tone (DMT). OFDM also forms the basis for the Digital Audio Broadcasting (DAB) standard in European Market [4].

<table>
<thead>
<tr>
<th>Table -1: Parameters of real OFDM system</th>
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<tbody>
<tr>
<td>Data rates</td>
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<tr>
<td>Modulation</td>
</tr>
<tr>
<td>Coding</td>
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<tr>
<td>FFT Size</td>
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<tr>
<td>Sub-carrier Frequency Spacing</td>
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<tr>
<td>FFT Period</td>
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<tr>
<td>Guard Duration</td>
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<tr>
<td>Symbol time</td>
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</table>

2.2 OFDMA (Orthogonal Frequency Division Multiple Access)

OFDMA is a multi user version of the popular OFDM digital modulation scheme. Multiple Access is achieved by assigning subsets of sub-carriers to individual users. This allows simultaneous low data transmission rate from several users. OFDMA is fast growing in several applications which are the heart of next generation of wireless communication. Apart from WiMAX, it is adapted for the IEEE 802.20 mobile Wireless MAN standard which is commonly referred as MBWA following to the Evolved UMTS Terrestrial Radio Access (E-UTRA). Figure 2-2, illustrates an overview of the Physical Layer (PHY) for WiMAX base-station with scalable OFDMA based on IEEE 802.16e-2005 [5].

![Fig-2: Overview of IEEE 802.16e-2005 Scalable OFDMA Physical Layer for WiMAX Base-stations](image-url)
3. PEAK TO AVERAGE POWER RATIO (PAPR) PROBLEM IN OFDM SYSTEM AND SOLUTIONS

In advanced mobile communication, OFDM has brought unique features such as high spectral efficiency, robustness to channel fading, immunity to impulse interference and capability of handling very strong multipath fading and frequency selective fading without having to provide power channel equalization [6]. On the other hand, an OFDM signal responses with higher instantaneous peak value with respect to the average signal level causing large amplitude swings when time domain signal travels from a low instantaneous power to high power waveform. As a result, unless the transmitter’s power amplifier exhibits an extremely high linearity across the entire signal level range, high Out-Of-Band (OOB) harmonic distortion of power waveform becomes significant which potentially causes interference with adjacent channel. That is why; large Peak to Average Power Ratio (PAPR) is marked as a major issue associated with OFDM signal generation which leads to system performance degradation due to distortions introduced by power amplifiers (PA) or other non-linear devices of the transmitter block.

3.1 PAPR Definition and Mathematical Representation

PAPR (Peak to Average Power Ratio) is a measurement of waveform, calculated from the peak amplitude of the waveform divided by the RMS value of the waveform. It implies that the PAPR is the maximum instantaneous power normalized by the average power among all possible data patterns. This definition is especially important for the system in which some special coding is employed that has some constraints in the data sequences control the PAPR very low. There thus appear two definitions largely accepted of PAPR for OFDM signal, one of that definition is to assume the PAPR can be expressed in deterministic value [7] [8], that is –

\[ D - \text{PAPR} = \sup_{-\infty < t < \infty} \zeta(t) = \sup_{0 \leq t \leq T} \max_{0 \leq t \leq T} \zeta(t) \ldots \ldots \ldots \ldots (1) \]

3.2 PAPR in OFDM System

The PAPR in OFDM system increases exponentially with the number of sub-carriers. To evaluate that, let, \( A = [A_0, A_1, \ldots, A(N-1)] \) to be modulated data sequences of the length \( N \) during the time interval of \([0,T]\), where \( A_i \) is a symbol from a signal constellation and \( T \) is the OFDM symbol duration. Then the complex envelope of the baseband OFDM signal for \( N \) carriers is given by [8],

\[ s(t) = \sum_{n=0}^{N-1} A_n \exp(j\omega_0 nt) \ldots \ldots \ldots \ldots \ldots \ldots \ldots (2) \]

Where, \( \omega_0 = \frac{2\pi}{T} \) and \( j = p-1 \)

In practical systems, a guard interval (cyclic prefix) is inserted by the transmitter in order to remove inter-symbol interference (ISI), and inter-channel interference (ICI) in multi-path environment. However in can be ignored since it does not affect PAPR The PAPR of the transmit signal \( s(t) \) in equation 2, is the ratio of the maximum instantaneous power and the average power [9], that is –

\[ \text{PAPR}(A) = \frac{\max |s(t)|^2}{E \{ |s(t)|^2 \}} \ldots \ldots \ldots \ldots \ldots \ldots \ldots (3) \]

Where, \( E \{ . \} \) denotes the expectation operator.

Usually the continuous time PAPR of \( s(t) \) is approximated using the discrete time PAPR shown in equation 3, is obtained from the samples of the OFDM signal.

3.3 Techniques to reduce PAPR in OFDM system

Several schemes have been proposed to reduce PAPR. These techniques can mainly be divided into two categories [6]. Those are –

A) The Signal Scrambling techniques are all variations

on how to scramble the codes (or modify the phases) to decrease the PAPR. Golay complementary sequences, Shapiro-Rudin sequences, M-sequences, Baker codes can be used to efficiently reduce the PAPR. However, with the increase in the number of carriers, the overhead associated with the exhaustive search or the best code would increase exponentially. More practical solutions of the scrambling mechanism are block coding, selective mapping and partial transmit sequences. Selective mapping and partial transmit sequences are two probabilistic schemes to reduce PAPR.

B) The Signal Distortion techniques reduce higher peaks directly by distorting the signal prior to amplification. Clipping the OFDM signal before amplification is a simple method to limit PAPR. More practical solutions are Peak Windowing, Peak Cancellation, Peak Power Suppression, Weighted Multi-Carrier transmission, Companding and Deliberate Clipping.

3.4 PAPR Reduction by Deliberate Clipping

If the number of subcarriers increases however, the peak-to-average power ratio (PAPR) of the OFDM signal also increases. In many wireless applications, both the peak power efficiency and the bandwidth efficiency are the two most important factors [10]. In strictly band-limited systems, the OFDM signal exhibits a prohibitively high PAPR; and without use of any PAPR reduction technique, efficiency of power consumption at the transmitter becomes very poor.
The deliberate clipping method may be one of the simplest solutions when the number of sub-carriers is large [11], [12]. The clipping operation causes degradation due to the nonlinear operation, which requires some compensation the deliberate clipping is performed followed by the band pass filter, and the resultant performance degradation is compensated by the BCH codes [13]. On the other hand, the OFDM signal sampled at the Nyquist rate is clipped and the degradation is compensated by the iterative decision-aided reconstruction of the original OFDM signals [14].

When the clipping is performed on the oversampled OFDM signals, it generally causes the out-of-band radiation of the clipped power, and the band pass filter is required to suppress the out-of-band radiation. The problem of this scheme is the significant PAPR regret due to the band pass filtering [11]. On the other hand, when the clipping is performed on the signals at Nyquist sampling rate, all the distortion noise falls in-band, avoiding the out-of-band radiation due to the deliberate clipping, assuming that the signal is linearly amplified [11], [14].

As a clipping model of the baseband signal, the soft envelope limiter block shown in figure 3 is considered as the function of clipping: the output sample is thus given by

\[
\hat{r}_n = g(r_n) = \begin{cases} r_n : r_n \leq A_{\max} \\ A_{\max} : r_n > A_{\max} \end{cases} \quad \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots (4)
\]

Where, \( \hat{r}_n = |s(n)| = \sqrt{(x_n^2 + y_n^2)} \) is the amplitude of the nth sample of complex OFDM signal and \( A_{\max} \) is the maximum permissible amplitude over which the signal is clipped. The clipping ratio \( \gamma \) is defined as,

\[
\gamma = \frac{A_{\max}}{\sqrt{P_{in}}} = \frac{A_{\max}}{\sqrt{2\sigma}} \quad \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots (5)
\]

Where, \( P_{in} = 2\sigma^2 \) is the input power of the OFDM signal before clipping.

The total output power \( P_{out} \), which is the sum of the signal and distortion components, is given by,

\[
P_{out} = E_{rn} \left[ g^2(r_n) \right] \quad \text{or}, \quad P_{out} = (1 - e^{-\gamma^2})P_{in} \quad \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots (6)
\]

Normalizing the clipped signal by the rms output power, the sample of the output amplitude is redefined as

\[
r_n = \frac{g(r_n)}{\sqrt{P_{out}}} = \frac{g(r_n)}{\sqrt{(1 - e^{-\gamma^2})P_{in}}} \quad \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots (7)
\]

It is to be noted that \( \gamma \) cannot be zero by the definition [16]. However, considering the amplitude normalized by the rms output power, it can be defined that \( \gamma \neq 0 \) by its limit as,

\[
\lim_{\gamma \to 0} r_n \leq \lim_{\gamma \to 0} \frac{A_{\max}}{\sqrt{P_{out}}} = \lim_{\gamma \to 0} \frac{\gamma}{\sqrt{(1 - e^{-\gamma^2})P_{in}}} = 1 \quad \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots (8)
\]

That is, \( r_n = 1 \) for all \( n \), which corresponds to the hard (constant) envelop limiter.
4. SIMULATION RESULTS OF PERFORMANCE ANALYSIS OF OFDM SIGNAL

In this section, result of the simulation study on the performance is discussed. To study and find the optimizations, an algorithm illustrated in figure 4, was simulated using MATLAB simulation software. The total analysis is divided into two different parts of which discussed in section 4.1 which deals to determination of optimum FFT size and cyclic prefix co-efficient by analyzing the bit error rate vs signal-to-noise ratio curves followed by results enlisted in section 4.2 which shows the difference or improvement of performance of the baseband OFDM signal while voltage clipping ratio is introduced and optimized.

To overcome the problem of the Inter Symbol Interference (ISI) another parameter is defined as the Cyclic Prefix (CP). For OFDM signal transmission with multiple carriers, CP is appended. Mathematically, the relation is illustrated below –

\[
\text{Cyclic Prefix Co-efficient} = G_i = \frac{T_{cp}}{T_d} \ldots \ldots \ldots \ldots (9)
\]

Where, \( T_{cp} \) = Cyclic Prefix Duration

\( T_d \) = Guard Duration

Cyclic Prefix Co-efficient or Gi is the ratio of guard duration to the cyclic prefix duration. While optimizing the FFT size, the Gi value was kept constant to 0.25.

The values of different parameters used in the simulation for optimization of FFT size is illustrated in table 2. The results are illustrated in

**Table-2:** Different Parameters used in the simulation for optimization of FFT Size

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modulation Scheme</td>
<td>QAM 16</td>
</tr>
<tr>
<td>FFT Size</td>
<td>4, 16, 64, 128</td>
</tr>
<tr>
<td>Data Sub-carriers</td>
<td>52</td>
</tr>
<tr>
<td>Guard Duration</td>
<td>64</td>
</tr>
<tr>
<td>Cyclic Prefix Co-efficient</td>
<td>0.25</td>
</tr>
</tbody>
</table>

Using the same simulation model, the optimum value of Cyclic Prefix Co-efficient was determined too. Table 3 shows the simulation model parameters for this optimization. For this investigation, the result of the FFT size optimization was kept constant.

**Table-3:** Different parameters used in simulation for optimization of Cyclic Prefix Co-efficient

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Modulation Scheme</td>
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<td>52</td>
</tr>
<tr>
<td>Guard Duration</td>
<td>64</td>
</tr>
<tr>
<td>Cyclic Prefix Co-efficient</td>
<td>0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9</td>
</tr>
</tbody>
</table>
Figure 5 illustrates the simulation results for optimizing FFT size for the baseband OFDM signal using QAM16 modulation technique. As the FFT size was varied through a range of values from 4 to 128, it was observed that initially the simulation results differed largely compared to theoretical results. When FFT size was increased to 64, there was significant improvement and for FFT size value 128, it was the near perfect output. But as the FFT size increases, it offers higher complexity in system designing for hardware implementation [18]. That’s why the optimum value for FFT Size is determined to be 64.

Determining the optimization for Cyclic Prefix Co-efficient, Gi the FFT size obtained by the illustration in Figure 5 was fixed at 64 and the similar simulation model was used. The Gi values were varied from 0.1 to 0.9. The analysis is illustrated on figure 6 where it is visually clear that BER to SNR curve improves with the increase to the value of Gi. The best optimizations were found in a range of 0.4 to 0.7 and for Gi=0.5, the results were closer to that of the theoretical values. As a result, the Cyclic prefix Co-efficient was best kept at Gi=0.5 for optimum performance.

4.1.2 Determination of Optimum Voltage Clipping Ratio (VCR)

The main objective of this paper is to study a special type of signal distortion type PAPR reduction scheme which is Deliberate Clipping which is performed by distorting the signal prior to amplification as illustrated in figure 3.

A significant advantage of clipping is it makes the transmission power efficient. However extensive clipping may cause large Out-of-Band (OOB) and In-band interference. That’s why it is highly required to investigate the clipping and understand its effect on overall performance of the baseband OFDM signal. The modified model for this simulation is illustrated in figure 7.

In the simulated model all the parameters i.e. Modulation, Data Sub-carriers are kept at the IEEE 802.16 standard [19]. The FFT size and Cyclic Prefix co-efficient is set according to the optimum value found in the earlier simulation illustrated in the section 4.1.1. In this paper, a term called “Voltage Clipping Ratio (VCR)” or Cp which is mathematically it is represented as –

$$C_p = \frac{|A_m|}{A}$$  \hspace{1cm} (10)

Where, \(A_m\) = \(A_{max}\) or \(A_{min}\) = Maximum or Minimum clipping voltage and \(A\) = Clipping threshold voltage. The value of VCR was varied in a range of 5% to 40% and observed in terms of the improvement of BER vs SNR curve with respect to earlier optimized results which were performed without clipping the signal. Table 4 lists the parameters for the modified model of simulation.

Table 4: Parameters to optimize the Voltage Clipping Ratio

<table>
<thead>
<tr>
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<th>Values</th>
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</thead>
<tbody>
<tr>
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</tr>
<tr>
<td>Guard Duration</td>
<td>64</td>
</tr>
<tr>
<td>Cyclic Prefix Co-efficient</td>
<td>0.5</td>
</tr>
<tr>
<td>Voltage Clipping Ratio (VCR)</td>
<td>5% - 40%</td>
</tr>
</tbody>
</table>
The results of simulation found by increasing VCR are shown in figures 8, 9, 10, 11, 12 and 13.
5. CONCLUSIONS

The nonlinear distortion effects in OFDM transmission have been investigated in many research works. An analytical expression for the output autocorrelation function based on HPA modeling with Bessel series expansion is derived. By using Fourier transformation, the output autocorrelation function can provide information on the power spectral density (PSD) at the HPA output, and at the same time, it allows the analytical calculation of the power of the nonlinear distortion noise [21]. The orthogonal polynomials provide an intuitive means of spectral re-growth analysis and enable us to derive a very simple analytical expression for the autocorrelation function and hence the PSD of the nonlinear noise. In this way, it is possible to derive an analytical BER expression for the OFDM systems performance in presence of nonlinear HPA in AWGN channels [20].

In this paper, in terms of observing the performance of OFDM based WiMAX system, we limited our study within reducing PAPR and improving the BER to SNR of OFDM signal by Deliberate Clipping technique. On the other hand, the OFDM signals are highly sensitive to non linear distortions introduced by the High Power Amplifier (HPA). It has two effects on transmission the first one, is the spectral re-growth of the signal which leads to adjacent channel interference (ACI) and the second one is the effect in the distortion of the signal in the nominal frequency band which causes inter-symbol interference (ISI).

Investigations in these directions are great attempts to optimize OFDM performance enhancement and it is a matter of utter satisfaction to conclude with the observations made throughout the research work.

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**BIOGRAPHIES**

Mazid Ishtique Ahmed received his B.Sc. in Electrical and Electronic Engineering degree from Ahsanullah University of Science and Technology, Dhaka, Bangladesh on 2010. For following two years, he served as an IT System Support and Solution Design Engineer in data edge limited, a system integrator and IT solution provider. He is in the position of Lecturer in Atish Dipankar University of Science and Technology and a graduate student in BRAC University, Bangladesh. His research interest includes Advanced Wireless Communication Technology fields of LTE and OFDM system implementation with performance enhancement solutions.

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