FUZZIFIED PSO FOR MULTIOBJECTIVE ECONOMIC LOAD DISPATCH PROBLEM

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Abstract

Power system engineers are always striving hard to run the system with effective utilization of real and reactive powers generated by the generating plants. Reactive power is used to provide better voltage profile as well as to reduce system losses. Membership functions are written for fuel cost, losses, stability index and emission release. As minimization of real power loss over the transmission lines, an attempt is made in this paper to optimize each objective individually using Fuzzy logic approach. In this paper basic assumption is Decision Maker (DM) has imprecise or fuzzy goals of satisfying each of the objectives, the multi objective problem is thus formulated as a fuzzy satisfaction maximization problem which is basically a min-max problem. The multi objective problem is handled using the fuzzy decision satisfaction maximization technique which is an efficient technique to obtain trade off solution in multi objective problems. The developed algorithm for Optimization of each objective is tested on IEEE 30 bus system. Simulation results of IEEE 30 bus network are presented to show the effectiveness of the proposed method.

Keywords: Real power, Reactive power, losses, membership functions, fuzzy logic and trade off solution

1 INTRODUCTION

The real power optimization sub-problem minimizes fuel cost by controlling controllable generator outputs while keeping the PV bus voltages unchanged. The system losses, stability index and emission computed at this power dispatch are very high compared with the results obtained when respective ones are taken as objective. Similarly the reactive power subproblem deals with minimization of total transmission loss of the system by controlling all the reactive power sources such as taps, shunts etc. Thus when loss minimization is taken as objective total system losses reduces but cost, emission and stability indices are high. The emission dispatch sub problem minimizes total emission output from the fossil fuel plants by controlling the generator outputs. At this power output of generator, the cost, total system losses and stability index are high. Similarly Stability index sub problem minimizes the index by controlling the PV bus voltages and thus improves the system stability limit. But the cost, emission and system losses are very high. Thus results of all the four sub problems are conflicting with one other. This can be inferred from previous chapters. In order to meet all the four objectives, we need a compromised solution which minimizes fuel cost, emission release, total transmission and losses and improved stability limit. This trade-off solution is obtained using a fuzzy decision satisfaction maximization method.

In this paper the data of four problems are fuzzified using fuzzy Min-Max approach and then Particle swarm optimization is used to determine the final trade off solution from all these Fuzzified values. This method is tested on IEEE 30 bus system and the results are presented.

2. PROBLEM FORMULATION

Each particle consists of power generations of all units excluding slack bus voltages, taps and shunts encoded in it. The size of each particle is equal to sum of active power generations, no of voltages excluding slack bus, number of voltage, taps, and shunts.

Assuming the decision maker (DM) has imprecise or fuzzy goals of satisfying each of the objectives, the multi objective problem can be formulated as a fuzzy satisfaction maximization problem which is basically a min-max problem. Our task over here is to determine the compromise solution for all the four optimization sub problems. Our goal is to minimize G(X) = compromised solution of $\{G_1(X_1), G_2(X_2), G_3(X_3), G_4(X_4)\}$

- While satisfying the set of constraints AX <B.
- Where $G_1(X)$ is Fuel cost minimization sub problem.
 - $G_2(X)$ is Loss minimization sub problem.
 - $G_3(X)$ is emission minimization sub problem.
 - $G_4(X)$ is index minimization sub problem.

- $F_2(X_i)$ be the losses in P.U for ith control vector
- $F_3(X_i)$ be the Stability index for ith control vector
- $F_4(X_i)$ be the Emission release in kg/hr for $i^{\text{th}}\,\text{control}\,\text{vector}$

Let $F_1(X_i)$ be the fuel cost in $hr for i^{th}$ control vector.

Let the individual optimal control vectors for the sub problems be X_1^* , X_2^* , X_3^* , X_4^* respectively. We have to find out a global optimal control vector X *such that

$$\begin{split} F_{1} \Big|_{X_{1}^{*}} &\leq F_{1} \Big|_{X^{*}} \leq F_{1} \Big|_{(X_{2}^{*}, X_{3}^{*}, X_{4}^{*})} \\ F_{2} \Big|_{X_{2}^{*}} &\leq F_{2} \Big|_{X^{*}} \leq F_{3} \Big|_{(X_{1}^{*}, X_{3}^{*}, X_{4}^{*})} \\ F_{3} \Big|_{X_{3}^{*}} &\leq F_{3} \Big|_{X^{*}} \leq F_{3} \Big|_{(X_{1}^{*}, X_{2}^{*}, X_{4}^{*})} \\ F_{4} \Big|_{X_{4}^{*}} &\leq F_{4} \Big|_{X^{*}} \leq F_{4} \Big|_{(X_{1}^{*}, X_{2}^{*}, X_{3}^{*})} \end{split}$$

$$(1)$$

The imprecise or fuzzy goal of the DM for each of the objective functions is quantified by defining their corresponding membership functions μ_i as a strictly monotonically decreasing function with respect to the objective function *f* where i=1 to 4. In case of a minimization problem,

 $\begin{aligned} \mu_i = 0 \text{ or tends to zero, if } f_i > f_i^{max} & \text{ and } \\ \mu_i = 1 \text{ or tends to } 1, \end{aligned}$

 $\text{if } f_i < f_i^{\min} \tag{2}$

Where f_i^{max} and f_i^{min} are the unacceptable and desirable level for respectively. In our proposed approach we have considered a simple linear membership function for f_i because none of the objectives have very strict limits. The membership function, μ_i for ith objective is depicted in Fig. 1.1



Figure 1.1 Membership function for ith objective

The membership function can be defined as

$$\mu_{i} = \frac{F_{i}^{\max} - F_{i}}{F_{i}^{\max} - F_{i}^{\min}} \qquad F_{i\min} \leq F_{i} \leq F_{i\max}$$

$$1 \qquad F_{i} < F_{i\min}$$
(3)

Using Eq. (3) the membership functions can be formulated as

2.1 Membership Function for Fuel Cost

$$\mu_{1} = \frac{F_{1}^{\max} - F_{1}(X)}{F_{1}^{\max} - F_{1}^{\min}} \qquad F_{1\min} \le F_{1} \le F_{1\max}$$

$$1 \qquad F_{1} < F_{1\min}$$

Where F_{1max} =max { $F1(X_1^*)$, $F1(X_2^*)$, $F_1(X_3^*)$, $F_1(X_4^*)$ } F_{1min} =min { $F1(X_1^*)$, $F1(X_2^*)$, $F_1(X_3^*)$, $F_1(X_4^*)$ }

(4)

2.2 Membership Function for Losses

$$\mu_{2} = \frac{F_{2}^{\max} - F_{2}(X)}{F_{2}^{\max} - F_{2}^{\min}} \quad F_{2\min} \leq F_{2} \leq F_{2\max}$$

$$1 \qquad F_{2} < F_{2\min}$$

(5)

Where $F_{2max} = max \{F2(X_1^*), F2(X_2^*), F_2(X_3^*), F_2(X_4^*)\}$ $F_{2min} = min \{F2(X_1^*), F2(X_2^*), F_2(X_3^*), F_2(X_4^*)\}$

2.3 Membership Function for Stability Index

(6)

Where
$$F_{3max} = max \{F3(X_1^*), F3(X_2^*), F_3(X_3^*), F_3(X_4^*)\}$$

 $F_{3min} = min \{F3(X_1^*), F3(X_2^*), F_3(X_3^*), F_3(X_4^*)\}$

2.4 Membership Function for Emission Release

$$\mu_{4} = \frac{F_{4}^{\max} - F_{4}(X)}{F_{4}^{\max} - F_{4}^{\min}} \quad F_{4\min} \leq F_{4} \leq F_{4\max}$$

$$1 \qquad \qquad F_{4} < F_{4\min}$$

Where $F_{4max} = max \{F4(X_1^*), F4(X_2^*), F_4(X_3^*), F_4(X_4^*)\}$ $F_{4min} = min \{F4(X_1^*), F4(X_2^*), F_4(X_3^*), F_4(X_4^*)\}$

The maximum degree of overall satisfaction can be achieved by maximizing a scalar λ , which is the intersection of the four fuzzy membership functions.

Therefore objective function is maximization of $\lambda = \max (\mu_1, \mu_2, \mu_3, \mu_4)$.

Where λ varies from 0 to 1.

3. PROPOSED ALGORITHM

The proposed solution strategy for the multi objective problem is shown in the following algorithm

- 1. Reading the system data.
- 2. Reading the values of fixed cost, loss, index, emission for each sub-problem.
- 3. Forming Ybus matrix and FLG matrix for Lindex calculation.
- 4. Forming B1 sub matrix. Decompose B1 by Cholesky decomposition.
- 5. Randomly population and velocities are initialized.
- 6. Set Pbest=0 and itercount=1.
- 7. Set particle count=1
- 8. Decoding the particle, then the Decoded particle gives the values of power generations, voltage, magnitudes, tap values and shunts.

- 9. Forming the Ybus and B2 sub matrix. Decompose B2 by Cholesky decomposition
- 10. Run FDC load flow and compute loss.
- 11. Compute emission cost, fixed cost, and index values.
- 12. Fuzzifying the fuel cost, loss, emission and index obtained in step (11) using equations from Eq. 4 to 7.
- 13. Calculating the evaluation value of each individual in the population using Eq.(8). Compare each individual's evaluation value with its P_{best} . If the evaluation value of each individual is better than the previous P_{best} , the current value is set to be P_{best} .
- 14. Incrementing the individual count by 1. If count < population size go to step (8).
- 15. The best evaluation value among the P_{bests} is denoted as g_{best} .
- 16. Modifying the member velocity V of each individual according to $v_i^{k+1} = k^*(w^* v_i^k + c_1^* rand_1^*(pbest_i - x_i) + c_1^* rand_1^*(pbest_i - x_i))$

$$x_{i}^{k+1} = x_{i} + v_{i}^{k}$$

17. Modifying the member position of each individual Pi according to

$$Pi^{(k+1)} = Pi^{(k)} + Vi^{(k+1)}$$

Pi^(k+1) must satisfy the constraints.

18. Incrementing iteration count by 1.If the number of iterations reaches the maximum,

then go to Step 19, Otherwise, go to Step 7

19. The individual that generates the latest g_{best} , is the required control vector for the final trade off solution. Print the results

4. CASE STUDIES AND RESULTS

4. 1 IEEE 30 Bus System

25 independent runs are made for each sub problem and the values of four factors considered at minimum value of each sub problem (data) over 25 independent runs are determined. These values for all sub problems are given in Table 1.1.

Table	1.1	results	of	various	sub	problems	and	final	trade	off	solution	for	IEEE 30) bus	svste	em
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Optimization Problem	Fuel Cost (\$/hr)	Losses (MW)	Stability Index	Emission (kg/hr)
Fuel cost minimization sub problem results	806.498033	10.583711	0.272369	381.671279
Losses minimization sub problem results	945.214704	4.328367	.272443	233.701959
Stability Index minimization sub problem	897.142571	33.557655	0.162446	375.611008
Emission minimization sub problem	932.094511	4.404039	0.267070	229.144834
Final trade off solution	926.200519	4.634725	0.266459	242.142237

System generation =288.034725, total load 283.4 MW. The control variables are given in table 1.2 and 1.3.and Final bus voltages, power generation, line index values are given in table1.4.

Table 1.2 Positions	of tap	changing	transformers
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S.No	From-To buses	Tap value
1	6-9	0.9
2	6-10	1.1
3	4-12	0.975
4	28-27	0.9875

Table 1.3 Shunt suceptance values

S.No	From-To buses	Shunt suceptance
1	10	1.009617
2	24	1.0



Figure 1.2 Gbest particles (λ) Vs Iterations

S.No	Voltage	Pau	Oran	Lindex
1.	1.000000	0.712626	-0.231329	0.000000
2.	1.003158	0.729346	-0.027326	0.000000
3.	0.991421	0.500045	0.130286	0.000000
4.	0.995914	0.349738	0.633051	0.000000
5.	1.013388	0.222398	0.008802	0.000000
6.	1.000000	0.365994	0.674902	0.000000
7.	1.004216	-0.000000	-0.000000	0.001359
8.	0.998299	-0.000001	-0.000000	0.004968
9.	1.065043	0.000114	-0.000000	0.091909
10.	1.042844	0.000594	-0.000001	0.111362
11.	1.065043	0.000000	0.000000	0.091909
12.	1.055699	-0.000930	-0.000005	0.114096
13.	1.045549	-0.000019	-0.000007	0.122494
14.	1.040786	-0.000015	0.000001	0.120544

Table 1.4 Final bus voltages, Power generations, Lindex

15.	1.036565	-0.000020	0.000002	0.118529
16.	1.027964	0.000961	0.000004	0.110391
17.	1.033049	0.000009	0.000002	0.113342
18.	1.025878	-0.000003	0.000001	0.126912
19.	1.023364	-0.000002	-0.000000	0.128017
20.	1.027458	0.000004	-0.000001	0.124354
21.	1.027112	0.000018	-0.000005	0.115108
22.	1.026608	-0.000500	-0.000001	0.114624
23.	1.026413	-0.000004	-0.000000	0.118209
24.	1.021240	0.000003	-0.000002	0.114837
25.	1.043109	-0.000003	0.000000	0.099710
26.	1.025885	-0.000002	-0.000000	0.105356
27.	1.064945	0.000067	-0.000003	0.089225
28.	0.992422	-0.000060	0.000000	0.012565
29.	1.045961	-0.000002	0.000000	0.104411
30.	1.034977	-0.000008	0.000001	0.118026

CONCLUSIONS

The final trade off solution is obtained. 25 independent runs are made for each sub problem and the optimal values of four objectives considered at minimum value of each sub problem over 25 independent runs are determined. In this work basic assumption made is that the decision maker (DM) has imprecise or fuzzy goals of satisfying each of the objectives, the multi objective problem is thus formulated as a fuzzy satisfaction maximization problem which is basically a minmax problem. The multi objective problem is handled using the fuzzy decision satisfaction maximization technique which is an efficient technique to obtain trade off solution in multi objective problems.

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