

# DESIGN OF THIN WALL STRUCTURES FOR ENERGY ABSORPTION APPLICATIONS: DESIGN FOR CRASH INJURIES MITIGATION USING MAGNESIUM ALLOY

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## Abstract

*This paper describes a computational investigation on the response of thin wall structures due to dynamic compression loading. In this paper, the tubes subjected for both direct and oblique loading. Several different cross-sectional structures have been studied to specify the best one. Initially the tubes were subjected to direct loading, and then the tubes were subjected to oblique loading. After that, the tubes were compared to obtain the cross section which fulfills the performance criteria. The selection was based on multi criteria decision making (MCDM) process. The performance parameters taken in this study are the specific energy absorbed by the tube for both direct and oblique, crush force efficiency and the ratio between the energy absorbed by direct and oblique loading. Trigger and foam filled are implemented to study their effects on the parameters used. The study used the magnesium alloy as a material to study potentially the possibility and ability of using the magnesium alloy in the energy absorber parts since the magnesium has lighter weight.*

**Index Terms:** dynamic compression, thin wall, energy absorption, direct oblique loading

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## 1. INTRODUCTION

It is known that thousands of people throughout the world are killed or seriously injured due to collisions every year.[1] showed the problem of causalities as a result of road accidents is acknowledged to be a global phenomenon in all countries around the world because of the growth in number of people. The dangerous comes from the impact energy that transmit to the car occupant and hence to the passengers. To keep passengers safe the impact energy transmitted to the passengers should be as low as possible. To minimize the impact energy it is necessary to dissipate the energy comes from collision by absorbing the energy through deformation of car structure; this will reduce the risk and hence will keep the passengers more safe. It is necessary to find out a method to increase the car structure members' ability to absorb impact energy as much as possible and allow an acceptable energy passes to the passengers. The structures are called frontal longitudinal as shown in Figure 1.

Many researchers have done to improve the energy absorption of these structures due to axial impact [2]. However in the context of a vehicle collision, the vehicles energy absorbers are commonly subjected to both axial and oblique (off-axis) loads. If compared with axial loading conditions, relatively few studies have been conducted on the energy absorption response of thin walled tubes under oblique loads [4]. Some of the well cited works in this oblique impact are works of Borvik et al. [5],

Reyes et al. [6-8] and Reid et al. [9]. When the vehicle is subjected to an oblique loading, the frontal longitudinal collapses in a bending mode rather than axial crush [10], this causes to lower energy absorption capability of the frontal longitudinal.

Some researchers have considered foams for energy absorption. Foam used as a filler which might be metallic or polymeric [11-17]. It was concluded that using of foam leads to increase the energy absorption capability for tubular structures and decreases the energy absorption stroke (crush length of tube). And this is useful especially when designing compact cars.







Recently, the researchers trend to the computer simulation (finite element analysis-FEA) instead of experimental work. FEA widely used for analysis and optimization. In impact studies, FEA has shown to be able and useful tools to understand the deformation and responses of the energy absorber tubes under impact loading [18, 19]. Using FEA reduces time and cost which may uses in the experimental work. The objective of this study is to design an efficient thin wall tube as an energy absorber by using finite element analysis

## 2. DESIGN METHODOLOGY

Six different walled tubular cross sectional profiles were designed. The profiles are circular, square, rectangular, hexagonal, octagonal and ellipse. The tubular structures

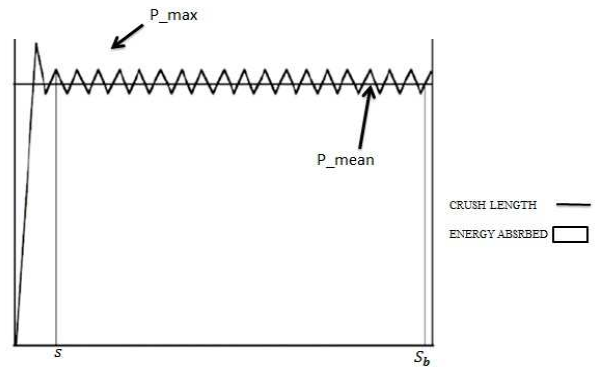
material was modeled as magnesium alloy (AZ31). The perimeter of the six profiles, the length and the thickness were kept constant. This was carried out just to investigate the various cross sectional profile crash performance. The length and the thickness were chosen to be 350mm and 2mm respectively. Two different perimeter lengths were chosen 300mm and 372 mm respectively. From these six profiles, one of them will be chosen by Multi Criteria Decision Making (MCDM) process. After that the study enhances the crash performance of the chosen profile. The foam filler material includes to that profile namely aluminium foam with density of 534kg/ m<sup>3</sup>. The dynamic simulations for tube and foam filled tube include direct and oblique loading (30 degrees off the tubular longitudinal axis). The initial velocity used in the simulations was 15m/s with an impact mass of 275 kg. The values of the velocity and mass are discussed in the next section. The values are given in Table 1.

**Table 1:** Geometry and dimensions of tubes used for study

Profile	Specimen ID	Perimeter (mm)	Length (mm)	Mass (kg)	Major Dimension (mm)	Thickness (mm)	Profile
Circular	C_300	300	350	1.7	Diam. = 95.5 Diam. = 118.1	2	
	C_372	372		2.0			
Rectangle	R_300	300	350	1.7	90 x 60 112 x 74	2	
	R_372	372		2.0			
Square	S_300	300	350	1.7	75 x 75 93 x 93	2	
	S_372	372		2.0			
Hexagonal	H_300	300	350	1.7	50 each side 62	2	
	H_372	372		2.0			
Octagonal	O_300	300	350	1.7	37.5 each side 46.5	2	
	O_372	372		2.0			
Ellipse	E_300	300	350	1.7	62,31 74,37	2	
	E_372	372		2.0			

**Peak Force, FMAX**

The peak force of a component is the highest load required to cause significant permanent deformation or distortion. The peak load is of concern for two reasons. The first is that at low-speed and low-energy impacts, it is desirable that no permanent deformation takes place, as this would be considered damage to the structure. Secondly the peak load is often the maximum load observed in the useful stroke of the energy absorbing device and as such has a direct importance on the loading of the vehicle occupant.



**Figure 2:** Force displacement characteristics [20]

**Energy Absorption, Es**

The energy absorption performance can be calculated from the load-displacement curve. Energy absorption EA is denoted as an integration of a load-displacement curve as shown in Figure 2.

$$EA = \int_0^{\delta_b} P \cdot d\delta \tag{1}$$

When **P** is an instantaneous crushing load, **δ<sub>b</sub>** is the length of crushing specimen. From the equation (1).

$$EA = \int_0^{\delta_b} P \cdot d\delta = P_m (\delta_b - \delta_i) \tag{2}$$

Where **P<sub>m</sub>** is the mean crushing load, **δ<sub>i</sub>** is the initial length of the crushing specimen. An ideal energy absorption could achieve a maximum force and keep it constant during the entire deformation length.

**Crush Force Efficiency, CFE**

The crush force efficiency (CFE) can be defined as a mean crushing force (**P<sub>mean</sub>**) divided by peak crushing load (**P<sub>peak</sub>**) as follows.

$$CFE = \frac{P_{mean}}{P_{peak}} \tag{3}$$

The crush force efficiency is very important parameter used to evaluate the performance of energy absorbing structures [21]. A value of unity of the energy absorber member represents an ideal energy absorber which represents a value of the crush force efficiency corresponding to the constant load-displacement curve [22], while the low values indicate happening of greater peaks of force during crushing [23]. Low values of crush force efficiency means high peaks force which

leads to increasing in acceleration and potential damage to the passengers during frontal impact which must be avoided. CFE is related to the structural effectiveness and it is an important measure for car structure to know how efficient it is [24]. High values of CFE are desirable and must be maximized and this can be obtained by decreasing the peak load. Introducing trigger mechanism is usually used to decrease the peak load and thus increases the CFE value. [25] Showed that the crush force efficiency can be increased by increasing the wall thickness of the tube.

**Specific energy absorption (S.E.A)**

The most significant features of the longitudinal members are the Specific energy absorption (SEA). Which is define as the energy absorbed (EA) per unit mass and can be denoted as follows.

$$SEA = \frac{EA}{m} \tag{4}$$

Where ( $m$ ) is the original undeformed mass (before impact). The specific energy absorption is a measure of energy absorption capability of a structural component. The higher values of (SEA) are an indicator of the light weight crush members [26]. The specific energy absorption is an indicator of how efficient the absorber is. So the term is used to compare the ability among absorbers. High value of specific energy absorption can be gotten by decreasing the absorber mass, since the specific energy absorption depends on the density of the absorber material. Researches done on the energy absorption behavior stated that the using of tubular concept is most efficient energy absorption concepts evaluated [27]. It was found that the use of foam-filled tubes will increase the unreformed tube mass. By using foam-filled specific energy absorption will increase and it also increase by increasing the foam density [28].

**Stroke efficiency**

The stroke efficiency of structure  $S_E$  is the ratio between the maximum energy absorber crush lengths to the original absorber length which can be expressed as follow.

$$S_E = \frac{d_{max}}{l} \tag{5}$$

Where  $d_{max}$  is the maximum crush length of the energy absorber at when the compaction occurs and the energy absorption is at in maximum level, and  $l$  is the original length of the absorber. Also it is a measure of how the performance of a structure reaches to the best possible performance [29]. A unity value of stroke efficiency represents the ideal case of the

energy absorber, but in reality the value is always less than unity. They also concluded that the stroke efficiency decreased rapidly when the wall thickness increased and it increased when the length increased.

For the multi criteria decision making (MCDM) process, the complex proportional assessment method (COPRAS) was chosen [30, 31]. This method was chosen for its simplicity in usage. The method assumes direct and proportional dependences of the significance and utility degree of the available alternatives under the presence of mutually conflicting criteria. It takes into account the performance of the alternatives with respect to different criteria and the corresponding criteria weights [30]. This method selects the best decision considering both the ideal and the ideal-worst solutions. The COPRAS method is a successful method to solve problems of design selection in many fields like construction, project management, and economy. This method consists of many steps, and they are explained as follows:

**Step 1: Developing the Initial Matrix (X) and Find the Relative Coefficient (R)**

This first step involves the generation of a simple matrix which maps the alternatives (design concepts) to the selection criteria. This matrix is labeled as X as given in equation3.

$$X = [x_{ij}]_{m \times n} = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1n} \\ x_{21} & x_{22} & \dots & x_{2n} \\ \vdots & \vdots & \vdots & \vdots \\ x_{m1} & x_{m2} & \dots & x_{mn} \end{bmatrix}$$

$(i = 1, 2 \dots m), (j = 1, 2 \dots n)$  (6)

Where  $x_{ij}$  is the performance value of  $i$ th alternative on  $j$ th criterion,  $m$  is the number of alternatives (design concepts) compared and  $n$  is the number of criteria. The problem in design selection is that most design criteria are not in the same dimensions or units. This makes selection a little harder. One way to overcome this is to convert the entire matrix X to a non-dimensionalized matrix R. This way, it is easier to compare between selection criteria. The entry  $x_{ij}$  represents the positive (absolute) value for each criteria and  $\sum x_{ij}$  is the summation for a number of positives decisions. The importance of the relative coefficient is to reduce the values of the criteria to make it easy for comparing. The symbol of the relative coefficient is R and it is formulated as

$$R = [r_{ij}]_{m \times n} = \frac{x_{ij}}{\sum_{i=1}^m x_{ij}} \tag{7}$$

**Step 2: Determining the Weighted Normalized Decision Matrix D.**

The sum of dimensionless weighted normalized values of each criterion is always equal to the weight for that criterion.

$$D = [y_{ij}] = r_{ij} \times w_j \tag{8}$$

Where rij is the normalized performance value of ith alternative on jth criterion and wj is the weight of jth criterion. as given in equation 6.

$$\sum_{i=1}^m y_{ij} = w_j \tag{9}$$

To determine or compute the individual weightage for each criteria wj, the following method can be used:

Compare two criteria at a time. Total comparison sets (N) is equal to  $N = \frac{n(n-1)}{2}$  where n is the number of selection criteria.

Amongst the two criteria being selected, the criterion which is more important is given a score of 3 whereas the criterion which is least important is given a score of 1. If both criteria are of equal importance, a score of 2 is given. Repeat this for all other criteria.

The total score obtain for each criteria is computed as

$$\sum_{i=1}^m N_{ij} = W_j$$

A relative emphasis weighting factor, wj, for each selection criteria is obtained by dividing the total score for each selection criteria (Wj) by the global total score  $\sum_{j=1}^m W_j = G$ . (Refer Table 2 for example)

**Step 3: Summing of Beneficial and non-Beneficial Attributes**

The beneficial and non-beneficial attributes are in the decision matrix. The greater beneficial attribute is better selection also the low value of non-beneficial attribute is better selection too. After specify these attributes, the next step is to separate these values by their sums. The sums of the attributes can be formulated as in equations below:

**Table 2:** Example of weight age setting

Selection Criteria	Number of Comparison Sets, $N = 5(5-1)/2 = 10$										$W_j$	$w_j$
	1	2	3	4	5	6	7	8	9	10		
A	3	3	2	2							10	10/40 = 0.25
B	1				2	1	2				6	6/40 = 0.15
C		1			2			2	1		6	6/40 = 0.15
D			2			3		2		2	9	9/40 = 0.225
E				2			2		3	2	9	9/40 = 0.225
Total, $\sum$											G = 40	1

$$S_{+i} = \sum_{j=1}^n y_{+ij} \tag{10}$$

$$S_{-i} = \sum_{j=1}^n y_{-ij} \tag{11}$$

Where y+ij and y-i-j are the weighted normalized values of both the beneficial and non-beneficial attributes respectively. The high value of S+i, the better is the design concept, and the lower the value of S-i, the better is the design concept. Just to note that  $\sum S_{+i}$  and  $\sum S_{-i}$  of the design concepts are always respectively equal to the sums of weights for the beneficial and non-beneficial attributes as expressed by the following equation

$$Sum_{positive} = \sum_{i=1}^m S_{+i} = \sum_{i=1}^m \sum_{j=1}^n y_{+ij} \tag{12}$$

$$Sum_{negative} = \sum_{i=1}^m S_{-i} = \sum_{i=1}^m \sum_{j=1}^n y_{-ij} \tag{13}$$

The summation equation 9 and 10 is always equals to one.

**Step 4: Relative Significance or Priority (Q)**

The higher value of the relative significance is the best choice. The relative significance can be denoted in the formula as below:

$$Q_i = S_{+i} + \frac{S_{-min} \sum_{i=1}^m S_{-i}}{S_{-i} \sum_{i=1}^m (S_{-min} / S_{-i})} \tag{14}$$

Where S-min is the minimum value of S-i

**Step 5: Determining the Quantitative Utility (UI)**

Calculation of qualitative utility ( $U_i$ ) which directly related to the ( $Q_i$ ) value as mentioned in equation. From the equation it can be observed that the quantitative utility is directly proportionate to the relative significance. The maximum relative significance value is denoted as  $Q_{max}$ .

$$U_i = \frac{Q_i}{Q_{max}} \quad (15)$$

### 3. DYNAMIC ANALYSIS

Finite element codes ABAQUS/Explicit version 6.10 has been used in this study to model the response of energy absorbers and hence the frontal car subjected to dynamic impact loading under full overlap, offset overlap and oblique loading. ABAQUS is capable to simulate problems in various ranges as structural field, thermal electrical analysis, heat transfer, soil mechanics acoustics and piezoelectric. In implicit, the simulations take several orders of magnitude fewer increments than an explicit simulation in spite of the cost per increment is much greater. Explicit methods require a small time increment. ABAQUS/Explicit that operates explicit dynamic is suitable to model high speed dynamic and this is costly to analyses by using implicit methods. ABAQUS/Explicit is suitable to analyze the transient dynamic of the structures which subjected to impact loading [4]. It is possible to solve complicated, very general, three-dimensional contact problems with deformable bodies in ABAQUS/Explicit. Problems involving stress wave propagation can be far more efficient computationally in ABAQUS/Explicit. Energy absorbers deform to absorb energy under quasi-static or dynamic loading. So ABAQUS/Explicit is used in this study to model nonlinear loading of the energy absorbers.

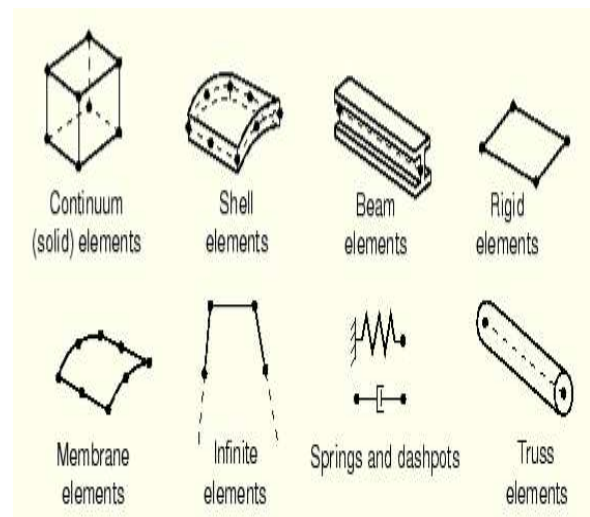
#### 3.1 Finite Element Modeling

In this study, finite element (FE) models of both empty and foam filled tubes were developed using the non-linear FE code ABAQUS-Explicit. The code was used to predict the response of the thin wall tubes subjected to a free falling impinging mass. The whole model comprises principally of the thin wall structure under study, the falling mass (striker), and the base. The thin wall structure was modeled by using 4 node shell continuum (S4R) elements with 5 integration points along the thickness direction of the element. The foam was modeled using 8-noded continuum elements with the reduced integration techniques in combination with hourglass control. Stiffness-based hourglass control was used to avoid artificial zero energy deformation modes and reduced integration was used to avoid volumetric locking. Elements size of 5 mm were chosen for the shells and foam elements, respectively, based on a mesh convergence study. A mesh convergence is important to ensure a sufficient mesh density to accurately capture the deformation process. The contact algorithm used to simulate contact

interaction between all components was the “general contact algorithm”. This is important to avoid interpenetration of tube wall. This algorithm is less intense in terms of computational time. Contact between the tube walls and tube walls with the foam were modeled as finite sliding penalty based contact algorithm with contact pairs and hard contact. The value of the Coulomb friction coefficient for all contact surfaces was set at 0.2 [25, 26].

The striker was modeled as a rigid body with only one allowable translational displacement while all other translational and rotations degree of freedom were fixed. The impact velocity of the striker on the tubes was modeled to be 15 m/s (54 km/h) with a lumped mass of 275 kg. (The impact speed value was taken based from the New Car Assessment Program (NCAP) by the National Highway Traffic Safety Administration (NHTSA). The mass was assumed to be 25% of a compact car (1100kg). It is assumed that each tubular energy absorbing structure is capable of absorbing an equivalent kinetic of 275 kg mass since in reality the maximum energy that can be absorbed by two tubes in service is much less than 50 % [33].

The wide range of elements is available in ABAQUS which are used to create the models. However, the extensive element library provides a powerful set of tools for solving many different problems, the figure (3) shows the type of element.



**Figure 3:** Commonly used element families in ABAQUS/Explicit (ABAQUS Version 6.6 documentation)

Shell element has been used to model thin-walled tube since shell element is suitable when the thickness of the tube is less than 1/10 of the height. All the absorbers have been modeled used in this finite element simulation were generated by using the element S4R. This element is a three-dimensional doubly

curved four node shell element. Each node has three-displacement and three-rotation degrees of freedom. While the two rigid plates modeled by using three-dimensional four-node rigid element R3D4. One of the two plates was fixed in all degree of freedom except in the direction of the applied load, while the other plate was fixed by constraining the whole degrees of freedom.

**3.2 Loading, Interaction and Boundary Conditions**

The tube was completely fixed to a rigid body (plate) from one end using tied constraint. This constraint makes the motion along with all displacement in linear and rotation degrees of freedom of all the nodes on the tube base edge the same of the rigid body. The plate was modeled as a rigid surface. Rigid surfaces are efficient analytical for contact simulations they are not element and don't need to specify masses, suction, and stress-strain. The other ends of the tube will constraint in all degree of freedom except in the direction of the moving impactor which will move axially towards the fixed plate. Two reference points will be defined, on the rigid plates, one on the fixed one which the reactions can be calculated and the second one will be defined on the moving plate (impactor) which at this point the masses and velocity can be defined.

Dynamic loading is simulated at the second reference point which mass and velocity have been defined. Step time can be defined in ABAQUS/Explicit by creating step and then by choosing dynamic, explicit and then specify the time period, long time period needs a long time to visualized the result and need high CPU capability. Period time depends on the nature of structure and also the mesh size.

Interaction has been done on all the parts of the structures. Interaction is available in ABAQUS/Explicit. For the tube walls and for the aluminium foam, self-contact between the walls must be defined while surface to surface contact should be defined between each rigid plate and the tube, between each part of telescope and another also between the tube and each part of telescope. Interaction option will be done after defining the contact surface and specify the friction coefficient "penalty". The surface-to-surface contact based on master-slave type. Constraints were done between the fixed rigid plate and the end of tube and between the fixed rigid and the end of the last part of telescope. That's mean contact can be done between deformable surfaces or between deformable surfaces and rigid surfaces. Mesh then defined by specify the mesh size 5mm size was used in this study according to [31], [32].

**4. RESULTS AND DISCUSSION**

Summary of the results obtain in this study is presented in Tables 5 – 6 for convenience. Detail discussions and explanations will be given in the accompanying sub sections.

**Table 5:** Summary of crashworthiness parameters for all tube profiles for two different parameters (direct loading)

Indicators	Circular		Rectangle		Square		Hexagonal		Octagonal		Ellipse	
	C-Direct 300	C-Direct 372	R-Direct 300	R-Direct 372	S-Direct 300	S-Direct 372	H-Direct 300	H-Direct 372	O-Direct 300	O-Direct 372	E-Direct 300	E-Direct 372
Energy (kJ)	14.5	14.8	10.4	11.6	11.4	12	14.5	16.6	14.2	16.4	12.8	14.2
Pmax (kN)	189	204	163	202	160	200	177	203	180	209	160	189
CFE	0.386	0.366	0.317	0.29	0.357	0.3	0.413	0.4	0.397	0.39	0.4	0.375
Faverage (kN)	73	74.7	51.7	58.4	57.1	60.4	73.2	80.6	71.5	82.4	63.9	70.9

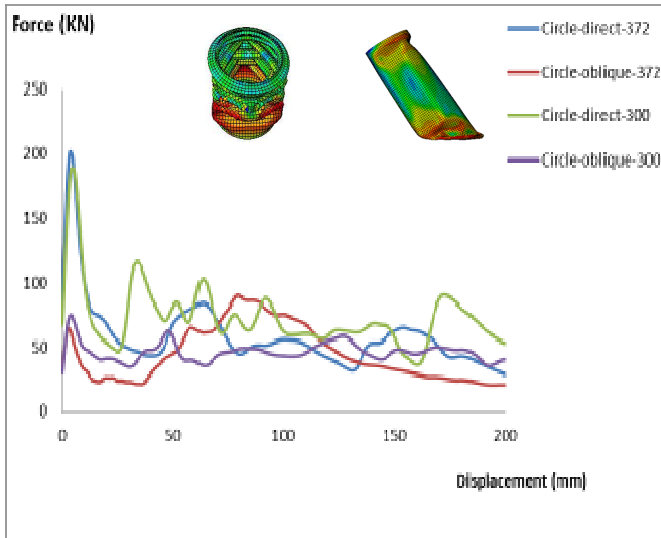
**Table 6:** Summary of crashworthiness parameters for all tube profiles for two different parameters (oblique loading)

Indicators	Circular		Rectangle		Square		Hexagonal		Octagonal		Ellipse	
	C-Oblique 300	C-Oblique 372	R-Oblique 300	R-Oblique 372	S-Oblique 300	S-Oblique 372	H-Oblique 300	H-Oblique 372	O-Oblique 300	O-Oblique 372	E-Oblique 300	E-Oblique 372
Energy (kJ)	9.2	8.6	6.7	7.3	7.3	7	9.8	10	9.3	10.4	8.3	10.5
Pmax (kN)	74.7	64.1	70.3	57.4	74.6	79.7	72.1	63.1	79.2	65	64.5	72.7
CFE	0.62	0.69	0.485	0.63	0.49	0.45	0.685	0.71	0.6	0.82	0.66	0.72
Faverage (kN)	46.3	44.6	34.1	36.4	36.7	35.9	49.5	44.6	48.1	53.4	42.5	52.9

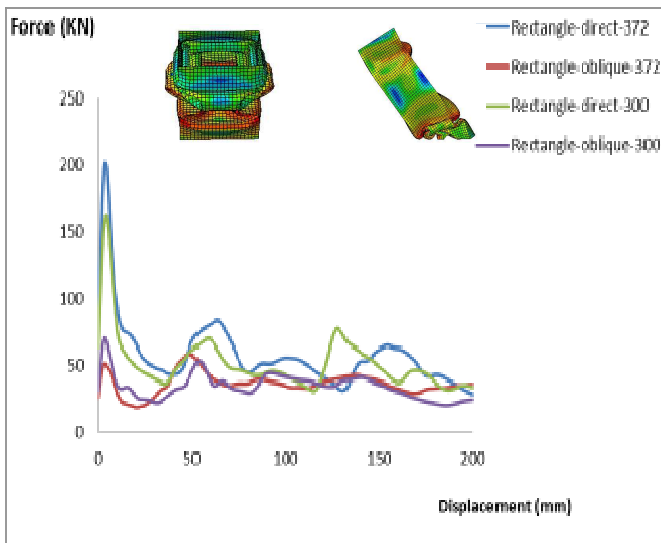
**4.1. Force Displacement Characteristics of different geometrical profiles**

Typical force displacement diagrams for each kind of profile tested in this study are presented in Figures 4 – 9. Each figure depicts the force response for certain cross sectional geometric profile due to the direct and oblique loading for the two classes of perimeters (300 mm and 372 mm respectively). From these figures, it is noticeable that the energy (area under the graph) absorbed by the tubes due to oblique loading is much lower than for direct loading. This is because the oblique loading causes two kinds of mechanical loads onto the tube. These loads are axial compression and bending. That is why the tubes under oblique loading bend while undergoing some form of progressive crushing. Besides this it is evident that the force displacement characteristic for different perimeter within a geometrical profile is rather similar for both axial and oblique

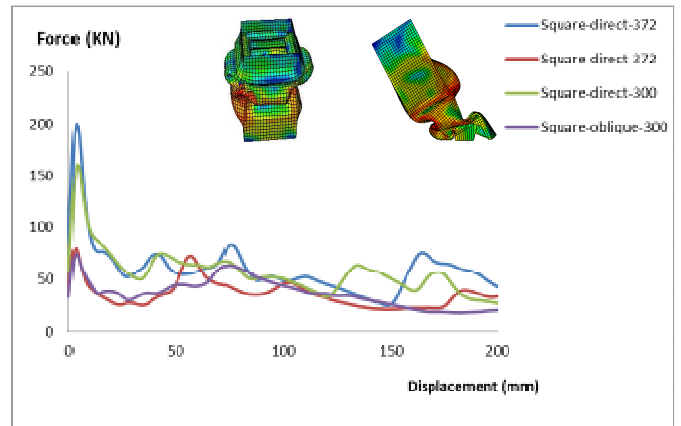
loading. This is an indication that the perimeter does not play an important role in the folding mechanism (progressive collapse) of the tubes.



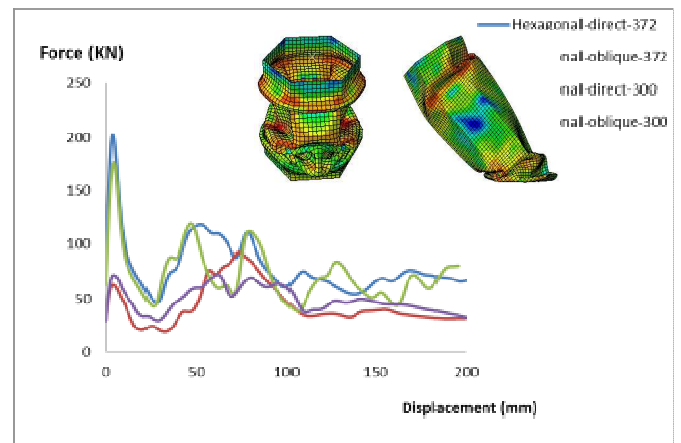
**Figure 4:** Force vs. displacement for circular tubes (direct and oblique impacts)



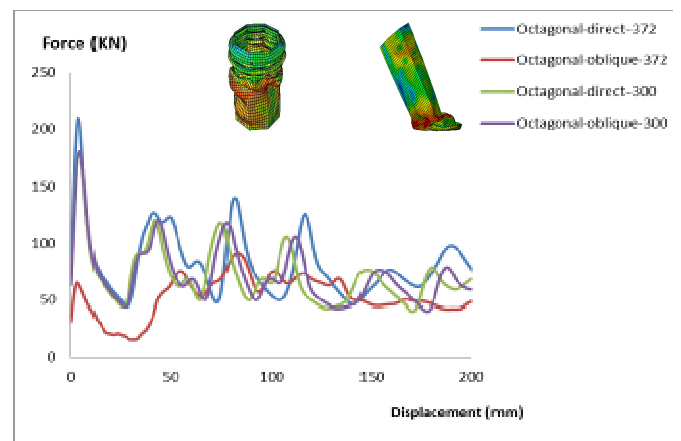
**Figure 5:** Force vs. displacement for rectangular tubes (direct and oblique impacts)



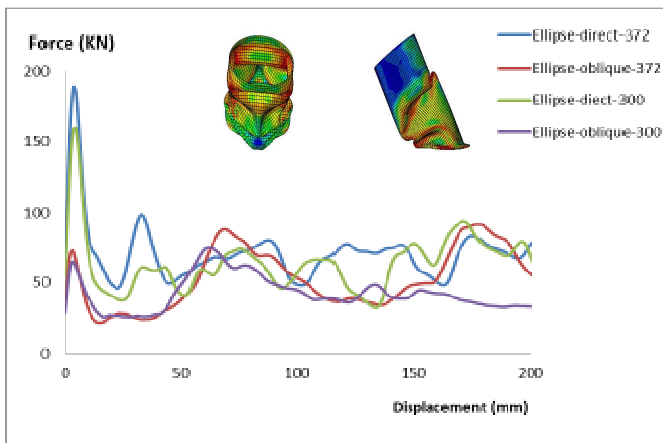
**Figure 6:** Force vs. displacement for square tubes (direct and oblique impacts)



**Figure 7:** Force vs. displacement for hexagonal tubes (direct and oblique impacts)



**Figure 8:** Force vs. displacement for Octagonal tubes (direct and oblique impacts)

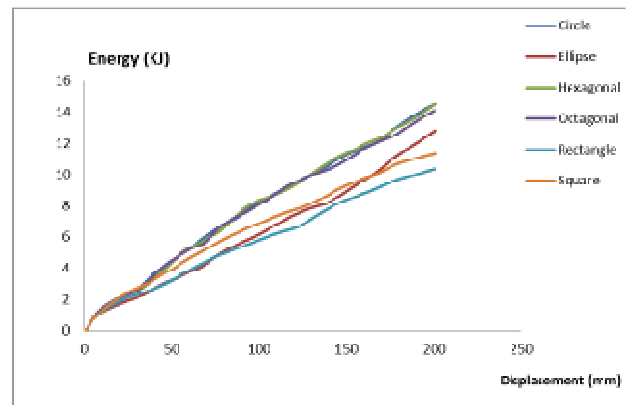


**Figure.9:** Force vs. displacement for Ellipse tubes (direct and oblique impacts)

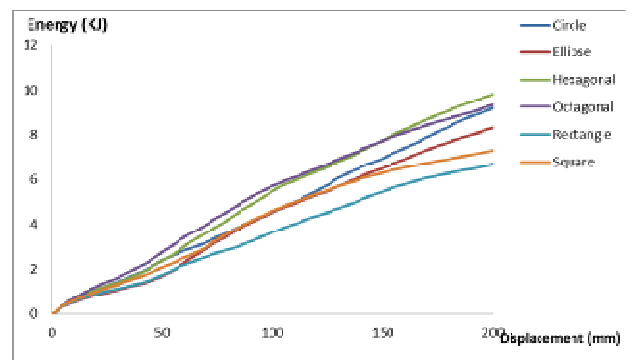
### 4.2. Energy Absorption

In Figures 10 and 11, the energy absorption is plotted as function of the deformation length rather than function of time because this facilitates the comparison of different structural design concepts. Based on these figures it can be concluded that rectangle cross sectional geometry has significantly lower energy absorption than the other five profiles for both impact conditions. Also from these figures, the octagonal and hexagonal profiles are better energy absorbers in both loading conditions. A summary of the energy absorption capabilities for all tube profiles are summarized in Figures 12 and 13 for both direct and oblique loading respectively. From here, it can be seen that as the perimeter was increased from 300 mm to 372 mm, most profiles exhibited a higher energy absorption capability. In terms of specific energy absorption (SEA), the hexagonal tube with a perimeter profile of 300 mm had the highest SEA compared to the other profiles. This is depicted in Figures 14 and 15 for direct and oblique loading respectively.

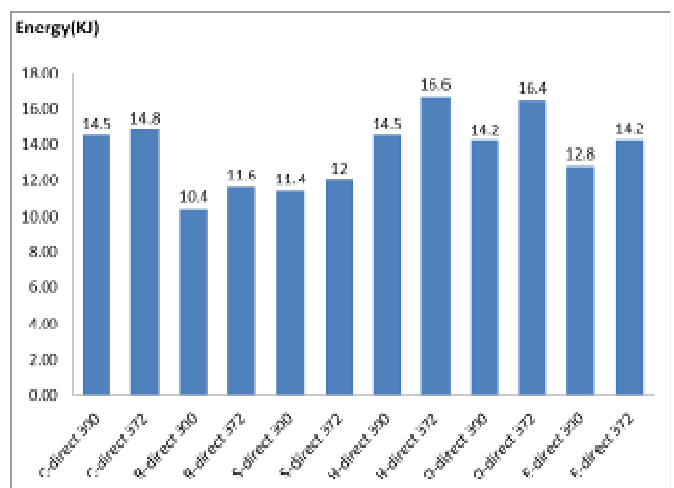
Another view of the energy absorption will be investigating the effects of profiles on the energy absorption due to oblique loading. This is depicted in Tables 7 and 8 respectively for both different perimeters under study. In general it can be concluded that profiles studied with oblique loading showed decreasing energy absorption. The percentage of decrease varies according to the profile type, but on an overall the difference is between 15 – 55 % for all profiles. Hexagonal, octagonal and circle are good geometry to be considered since they perform outstanding in terms of energy absorption in both loading and perimeter conditions respectively. The task now is to select the best tube in terms of the geometry profile and also the perimeter. This involves using performance criteria such as energy absorption capabilities; crush force efficiency, cost and manufacturing constraints. This will be discussed next.



**Figure 10:** Energy absorption characteristics of six different profiles for direct impact loading with perimeter 372 mm



**Figure 11:** Energy absorption characteristics of six different profiles for oblique impact loading with perimeter 300 mm



**Figure 12:** Energy absorption capability for various profiles due to direct loading condition.



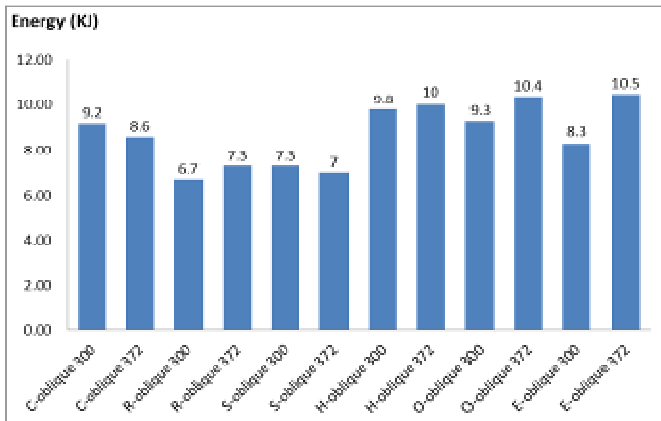


Figure 13: Energy absorption capability for various profiles due to oblique loading condition.

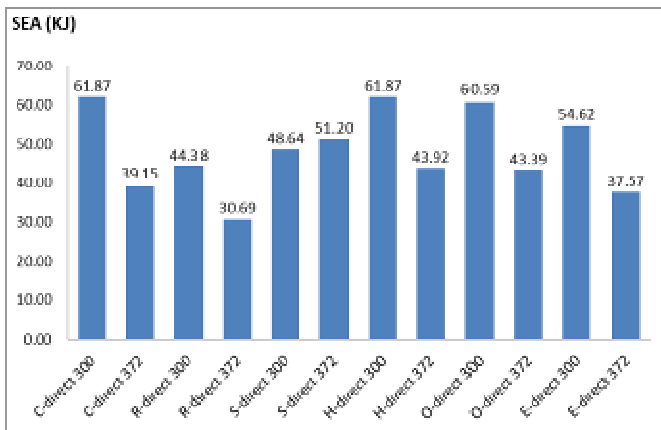


Figure 14: Specific energy absorption capability for various profiles due to direct loading condition.

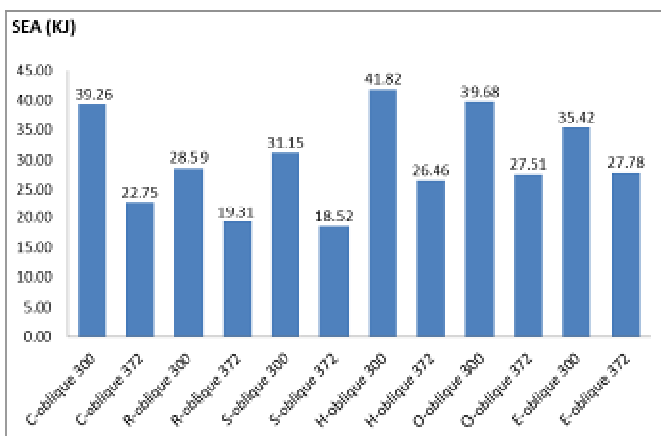


Figure 15: Specific energy absorption capability for various profiles due to oblique loading condition.

Table 7: Energy absorption of six profiles with three two different load conditions

Shape	Perimeter 372 mm	
	Energy absorption (kJ) Direct Impact 200 mm deformation	Energy absorption (kJ) Oblique Impact 200 mm deformation
Circle	14.8	8.6 -41.9%
Rectangle	11.6	7.3 -37%
Square	12	7 -41.7%
Hexagonal	16.6	10 -39.7%
Octagonal	16.4	10.4 -36.6%
Ellipse	14.2	10.5 -26%

Table 8: Energy absorption of six profiles with three two different load conditions

Shape	Perimeter 300 mm	
	Energy absorption (kJ) Direct Impact 200 mm deformation	Energy absorption (kJ) Oblique Impact 200 mm deformation
Circle	14.5	9.2 -36.5%
Rectangle	10.4	6.7 -35.5%
Square	11.4	7.3 -36%
Hexagonal	14.5	9.8 -32.4%
Octagonal	14.2	9.3 -34.5%
Ellipse	12.8	8.3 -35.1%

### 4.3. Selection of Best Profile

For the multi criteria decision making (MCDM) process, the complex proportional assessment method (COPRAS) was chosen. This method was chosen for its simplicity in usage. The method assumes direct and proportional dependences of the significance and utility degree of the available alternatives under the presence of mutually conflicting criteria. It takes into account the performance of the alternatives with respect to different criteria and the corresponding criteria weights. This method selects the best decision considering both the ideal and the ideal-worst solutions. The details of this method have been presented in the previous section. The first step is to determine the associated weightage for each performance criteria. This is depicted in Table 9. Once the weightages have been assigned to the respective indicators, the decision matrix, as shown in Table 10 is normalized using Eq. (7) and the corresponding weighted normalized decision matrix is developed, as given in Table 11.

The purpose of normalization is to obtain dimensionless values of different performance indicators so that all these criteria can be compared. This is followed by the computing the sums of the weighted normalized values for both the beneficial attributes and non-beneficial attributes as given in Table 12. In this case the only non-beneficial attribute is the ratio indicator where a lower value is preferred. Then, applying Eq. (14) the relative significance or priority value (Qi) for each tube concept is determined, as shown in Table 13. Table 13 also exhibits the value of quantitative utility (Ui) for each tube concept on the basis of which the complete ranking of the tube concept is obtained. The candidate tube for designing an efficient energy absorber is hexagonal with a perimeter of 300 mm, followed by hexagonal with a perimeter of 372 mm. The worst concept is the square profile. Hence, it is the hexagonal tube with a perimeter of 300 mm that was chosen for the next phase of study which is to investigate the effects of thickness and foam filling in the enhancement of energy absorption.

**Table 9:** Weightage setting for each performance indicator

Performance indicators	RUMS, $N = n(n-1)/2$ (n = number of performance indicators)										$\Sigma$	$\Sigma$
	1	2	3	4	5	6	7	8	9	10		
A.E(D) KI	2	3	3	2							10	0.
A.E(O) KJ	2				5	3	2				10	0.
C.F.E(D)		1			1		2	2			6	0.
C.F.E(O)			1			1	2		2		6	0.
Ratio				2			2	2	2	2	8	0.

A.E(D)	0	Energy absorbed (direct loading)	E =	40
A.E(O)	0	Energy absorbed (oblique loading)		
C.F.E(D)	0	Cross force efficiency (direct loading)		
C.F.E(O)	0	Cross force efficiency (oblique loading)		
Ratio	A.E(D)/A.E(O)			

**Table 10:** Data of performance indicators in a decision matrix

Specimens	Weightages				
	0.25	0.25	0.15	0.15	0.2
	Performance indicators				
	S.L.A (D)	S.L.A (O)	CFE(D)	CFE(O)	Ratio
C_300	61.87	39.26	38.6	62	1.57
C_372	39.15	22.75	36.6	69.5	1.72
R_300	44.38	28.59	31.7	48.5	1.55
R_372	30.69	19.31	29	63	1.59
S_300	48.64	31.15	35.7	49	1.56
S_372	51.2	18.52	30	45	1.71
H_300	61.87	41.82	41.3	68.5	1.48
H_372	43.92	26.46	40	71	1.66
O_300	60.59	39.68	39.7	60	1.52
O_372	43.39	27.51	39	82	1.57
E_300	54.62	35.42	40	66	1.54
E_372	37.57	27.78	37.5	73	1.35

**Table 11:** Weighted normalized decision matrix

Specimens	Weightages				
	0.25	0.25	0.15	0.15	0.2
	Performance indicators				
	A.E(D)	A.E(O)	CFE(D)	CFE(O)	Ratio
C_300	0.0267	0.027	0.013	0.0122	0.0166
C_372	0.0169	0.015	0.0125	0.0137	0.0182
R_300	0.0191	0.019	0.0108	0.0096	0.0164
R_372	0.0132	0.013	0.0099	0.0124	0.0168
S_300	0.021	0.021	0.012	0.0097	0.0165
S_372	0.022	0.0129	0.010	0.0089	0.0181
H_300	0.026	0.0291	0.014	0.0135	0.0157
H_372	0.019	0.0184	0.013	0.0140	0.0176
O_300	0.026	0.027	0.0135	0.0118	0.0161
O_372	0.018	0.019	0.0133	0.0162	0.0166
E_300	0.023	0.024	0.0136	0.0130	0.0163
E_372	0.016	0.0193	0.0128	0.0144	0.0143

**Table 12:** Sums of the weighted normalized values

Specimens	Beneficial Si+	Non-Beneficial Si-
C_300	0.079	0.018
C_372	0.059	0.015
R_300	0.059	0.014
R_372	0.049	0.016
S_300	0.064	0.021
S_372	0.054	0.022
H_300	0.083	0.016
H_372	0.065	0.019
O_300	0.079	0.019
O_372	0.067	0.016
E_300	0.075	0.012
E_372	0.063	0.013
$\Sigma$	0.8000	0.2000

**Table 13:** Qi and Ui values

Specimens	Q	U	Rank
CIR_300	0.094	94.1	3
CIR_372	0.077	76.7	10
Rec_300	0.079	78.5	8
Rec_372	0.066	65.7	12
Sq_300	0.0776	77.1	9
Sq_372	0.066	66.1	11
Hex_300	0.1	100	1
Hex_372	0.079	79	7
Oct_300	0.093	93	4
Oct_372	0.084	84	5
ELL_300	0.098	97	2
ELL_372	0.084	83.3	6

#### 4.4 Effect on Foam On Energy Absorption

In this phase of study, the selected tube from phase 1, namely the hexagonal tube with a perimeter of 300 mm was further investigated in terms of tube wall thickness and foam filling. The wall thickness selected were 1mm, 2mm and 3 mm respectively. Table 14 shows that the using of foam enhances both energy absorption and CFE, increases energy from 14.5 KJ to 60.2 KJ for the same deformation length.

**Table 14:** Effect of using foam and trigger on the magnesium tube subjected to axial loading

profile	hexagonal	With foam	With trigger
Energy absorption	14.5 KJ	60.2 KJ	13.85 KJ
CFE	41%	52 %	44.7 %

#### 4.5 Effect on Trigger Mechanism

Circular, square and elliptical were used in this study. Circular trigger shown the best values. It was shown that the distribution of holes in non-neighbors side is the best choice. These six holes distributed on three sides as two holes in each side. Three reduction percentage also used 5, 10, 15% the 10% reduction shows the best selection. Different trigger position used, 10, 20, 30, 40, 50, 60 and 70 mm of the edge used, the 50mm of trigger location reveals the best selection.as shown in table 14 the trigger increase the CFE by 9% . Using trigger decreases the peak load by 12.5% which decreases the force transmitted to the passengers.

## CONCLUSIONS

A numerical investigation of both the axial and oblique crush response of thin walled has been done. Ductile metallic Magnesium alloy (AZ31) of various cross sectional profiles was performed. The investigation was broken up into three phases: (1) the investigation of individual cross sectional profile and the selection of the best profile, (2) the investigation of tube foam filling on the crush response on the chosen profile and finally (3) the effect of trigger mechanism onto the selected profile design. All simulations were dynamic with an impact speed of 15 m/s and impact mass of 275 kg. Oblique loading was simulated at a 30deg angle to the tube's axial direction. It was found that the hexagonal profile was a better concept for energy absorption application taking into accounts the crash performance indicators as well as the cost and manufacturing feasibility. The 2 mm thickness hexagonal tube had energy absorption of 14.5 kJ and a CFE of 0.41 for direct loading and 9.8 kJ and CFE of 0.68 for oblique loading respectively. When foam filling was added, the crash performance indicators improved. For direct and oblique loading, the 2 mm thickness hexagonal tube had energy absorption of 60.2 kJ and a CFE of 0.52for direct and 29.5 KJ and 0.86 for oblique loading. This is a mark improvement for the oblique impact crush performance. Finally, the trigger mechanism in form of a hole induced in the tube, helped to lower the peak force and improve the crash force efficiency from 0.41to 0.447 and reduces the peak force from 177KN to 155 KN in direct loading. This is partly due to the more effective progressive crushing that was introduced by the trigger mechanism. In conclusion, it can be said that the hexagonal tube of wall thickness 2 mm and with aluminum foam filling and a trigger mechanism has shown to be a good potential energy absorber candidate for crashworthiness application in helping mitigating serious injuries to the occupant of the vehicle.

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